Gearing Up for Geometry!

Geometry is right around the corner and you need to make sure you are ready! Many of the concepts you learned in Algebra I will be used in Geometry and you will be expected to remember them. Please take some time this summer and work through this review packet. Refreshing your memory of the concepts learned in Algebra I will help you hit the ground running in Geometry in the fall. Even though no one likes to do "homework" over summer vacation, putting in a little time up front will definitely help pay off next year. This packet is designed to take about a couple hours to do the entire thing so spread out the work. If you do a little each day, it will be done in no time! It will be collected next fall by your Geometry teacher on FRIDAY, September 7th. Have a great summer and we look forward to seeing you in September!!

Topics Covered in Algebra I that you need to know for Geometry

- ⇒ Solving Linear Equations
- ⇒ Solving Systems of Equations
- ⇒ Factoring
- ⇒ Solving Quadratic Equations
- ⇒ Simplifying Radicals

⇒ Distance Formula
 ⇒ Midpoint Formula
 ⇒ Pythagorean Theorem
 ⇒ Graphing Lines
 ⇒ Writing Equations of Lines

Plus more!!

Topics Covered in Middle School that you need to know for Geometry

Lots of what you will learn in Geometry next year has already been introduced to you during your elementary and middle school math experiences. A basic understanding of shapes, terminology, and simple area and volume formulas in addition to a good memory of concepts learned in Algebra I will keep you on the road to success in Geometry.

Thinking Skills Needed for Geometry

Geometry requires a different type of thinking than Algebra I. Algebra I is mostly a procedural course. A step-bystep method is taught for how to solve a particular problem and you get lots of practice mastering these skills on similar problems. In Geometry, success depends more on your ability to think logically and figure out problems that you may not have seen an exact replica of before.

- Spatial relation skills
- Problem solving skills
- Logical thinking



SOLVING EQUATIONS

Solving Linear Equations: SHOW ALL WORK and NO DECIMAL ANSWERS!			
1. $x + 3 = 23$	2 . 19 = <i>y</i> −15	3 . 24 = 3 <i>a</i>	
4. $44 = -4w$	5. $\frac{1}{3}k = -2$	6. $30 = -\frac{4}{3}w$	
7. $5x + 3 = 23$	8 . $8 - 5w = -37$	9. $\frac{x}{2} + 4 = 3$	
10. $4x - 9 = 7x + 12$	11. $5x - 22 - 7x + 2 = 40$	12. $2x = x + 3$	
13. $4(180 - x) = 90 - x$	14. $2(180 - x) + 45 = 3x$	15. $2(90 - x) + 180 - x = 45$	

16. $\frac{4}{3}x + 2(3 - x) = 5$	17. $2x - 3(x + 4) = -1$	18. $\frac{2x-5}{7} = 4$
19. $8(y-2)+6=2(y+1)$	20. $\frac{1}{2}z - \frac{3}{4} = z - \frac{5}{8}$	$21 3x + 4 = \frac{1}{3}x - \frac{8}{3}$

Solving Proportions: SHOW ALL WORK and NO DECIMAL ANSWERS!

Remember to solve proportions using cross multiplication. Here is an **EXAMPLE** if you are stuck:

$$\frac{2+x}{5} = \frac{3x-1}{9}$$

$$\frac{9}{9}(2+x) = 5(3x-1)$$

$$\frac{8+9x}{8} = 15x-5$$

$$\frac{8}{2} = 6x-5$$

$$\frac{23}{2} = 6x$$

$$x = \frac{23}{6} OR 3\frac{5}{6}$$

22. $\frac{5}{k} = \frac{7}{16}$	23. $\frac{a}{6} = \frac{-5}{2}$	24. $\frac{2k}{3} = \frac{k+1}{2}$	25. $\frac{j+3}{-5} = \frac{j-2}{3}$

SOLVING SYSTEMS OF EQUATIONS



	· -
y = -2x + 5	x + 4y = 5
3x - 2y = 4	5x - 7y = -2
	J
Solve using the FLIMINATION method. Solutions must be	e written as an ordered pair, no solution Ø, or the equation
of the line	
Here are two EXAMPLES if you are stuck:	
Try to eliminate one of the variables by adding or subtracting the equation	s. Sometimes the equations are all set for you like EXAMPLE A, but then
there are those like EXAMPLE B when you will need to force one of the va	riables to eliminate by multiplying each equation by a number.
, 	
x + y = 5	P $2x + 4y = -18$ P $2x + 4y = -18$
1	D. $3r - v - 1$ $A(3r - v - 1)$
+x-y=1	3x - y - 1 v $4(3x - y - 1)$
2x = 6	i de la companya de l
-	2x + 4y = -18
x = 3	+12r - 4v = 4
	$-\frac{112x}{-7y-7}$
Now that you know x, you can just plug x into either equation	14x = -14
to find the value of v	x = -1
	<i>"</i> -
(2) + n = 5	
(3) + y = 3	Now that you know x, you can just plug x into either equation to find the
y = 2	value of y.
Ť	
	2(-1)+4y=-18
SOLUTION: $(3, 2)$	2 + 4 - 19
	-2+4y = -18
	4 v = -16
•	
i	y = -4
	SOLUTION: (-1, -4)
•	
2	
2x + y = 1	$\begin{array}{c} x - 2y = 0 \\ 31 \end{array}$
3x - y = 14	x - 3y = 4



*****MULTIPLYING BINOMIALS—FOIL*****

FOIL- Multiply the FIRST terms, then the OUTER terms, then INNER, and finish with the LAST terms of each grouping. Combine all like terms for your final answer. Here is an EXAMPLE if you are stuck: $(x + 2)(x - 3)$ $x^2 - 3x + 2x - 6$ $x^2 - 1x - 6$			
36. $(x + 2)(x - 2)$	37. $(x-1)^2$	38. $(4x + 5y)(2x - 7y)$	

FACTORING



<u>Trinomials</u> When you factor a trinomial, make sure you find numbers that multiply to the last term and add to the middle term. Watch your signs! FOIL your answer to check! Here are two EXAMPLES if you are stuck:			
No number in front of the square $c^2 + 8c + 12 = (c+6)(c+6)(c+6)(c+6)(c+6)(c+6)(c+6)(c+6)$	No number in front of the squared term: $c^{2} + 8c + 12 = (c + 6)(c + 2)$ Number $3x^{2} + 3x^{2} +$		in front of the squared term: $4x - 7 \neq (3x + 7)(x - 1)$
45. $x^2 - 10x + 21$	46. $c^2 + c - 42$		47. $a^2 - 6a + 8$
48. $x^2 + 18x + 81$	49. $9x^2 - 12x + 4$		50. $25x^2 + 80x + 64$
51. $2x^2 + 5x + 2$	52. $5a^2 - 11a + 2$		53. $15k^2 - k - 2$

SOLVING QUADRATICS

Solving Quadratic Equations by Factoring

STEPS for solving a quadratic equation, $ax^2 + bx + c = 0$, by factoring:

- 1. Get the equation equal to zero
- 2. Factor
- 3. Set each factor or part equal to zero
- 4. Solve each equation algebraically to get the two solutions.

The factoring is mixed in the practice problems below. Here is an **EXAMPLE** if you are stuck:

$$x^{2} + 2x - 15 = 0$$

(x+5)(x-3)=0
x+5=0
x-3=0
x=3

These 3 examples are already factored for you—just solve!			
54. $(x-3)(x+2) = 0$	55. $(2x + 5)(3x - 1) = 0$	56. $7x(3x-2) = 0$	
Factor and Solve! You should have 2	answers for each.		
57. $2x^2 + 6x = 0$	58. $x^2 - 9 = 0$	59. $x^2 - x - 12 = 0$	
$60. \ 2x^2 + 3x - 2 = 0$	61. $x^2 + 2x - 15 = 0$	62. $x^2 + 6x + 9 = 0$	
$x^2 - 4x^2 = 0 = 0$	$x^2 + 14x = -40$	$x^2 + 5x - 150$	
63. 4x - 9 = 0	04. x + 14x49	63. $x + 5x = 150$	
66. $x^2 - 19x = 0$	67. $25x^2 = 1$	68. $3m^2 - 14m - 5 = 0$	



SIMPIFYING RADICALS—NO CALCULATORS THAT DO THE WORK FOR YOU!



Simplify radical expressions: Break down a radical expression by finding the LARGEST perfect square that divides out of the number under the square root. You might want to review perfect squares: List the largest perfect squares up to and including 225: Here is an **EXAMPLE** if you are stuck: $\sqrt{50}$ $\sqrt{25} \cdot \sqrt{2}$ Simplify the following radical expressions. NO DECIMAL ANSWERS! **72.** $\sqrt{20}$ 71. $\sqrt{12}$ **73**. √72 74. $\sqrt{200}$ 77. $\sqrt{8} \cdot \sqrt{6}$ 78. $\sqrt{5} \cdot \sqrt{15}$ 75. $5\sqrt{90}$ 76. $2\sqrt{12}$

Dividing radical expressions:

You may not leave a radical expression in the denominator of a fraction. If you have a radical in the denominator, you will need to RATIONALIZE THE DENOMINATOR.

Here is an **EXAMPLE** if you are stuck:



Simplify the following radical expressions. NO DECIMAL ANSWERS!

83. $\frac{1}{\sqrt{2}}$	84. $\frac{1}{\sqrt{7}}$	85. $\frac{3}{\sqrt{5}}$	86. $\frac{4}{\sqrt{3}}$

Distance Formula:

Use the distance formula when you want to find the length of a line segment or the distance between 2 ordered pairs.

$$D = \sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$$

Find the distance between each set of ordered pairs. Simplify any radical expressions. NO DECIMAL ANSWERS!				
87. (9, 7) and (1, 1)	88. (0, 6) and (-3, -2)	89. (5, 2) and (8, -2)		

Midpoint Formula:

Use the midpoint formula when you want to find the midpoint of a line segment with the specified endpoints. Write your answer as an ordered pair.

$$Midpoint = \left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$$

Find the midnoint between each set of orde

This the mapoint between each set of ordered pairs.			
90. (2, 4) and (6, 8)	91. (0, 6) and (-3, -2)	92. (-2, 6) and (8, 6)	



Pythagorean Theorem: Use the Pythagorean Theorem to find a missing side of a right triangle.



LINEAR EQUATIONS



Graphing Linear Equations:

For the following linear equations, determine the slope and y-intercept. Then graph the lines on each coordinate plane. See the example below to help if you have forgotten slope-intercept form from Algebra I:







110. $(2, 3)$ and $(2, 7)$	111. $(-1,0)$ and $(-3,-1)$	112. $(2, -5)$ and $(-2, 3)$

<u>Practice Standardized Test Questions:</u> Multiple Choice. A calculator may be used!

Do Your Figuring Below

1. Lisa has 5 fiction books and 7 nonfictions books on a table by her front door. As she rushes out the door one day, she takes a book at random. What is the probability that the book she takes is fiction?

А.	1
	$\overline{5}$
В.	5
	7
C.	1
	$\overline{12}$
D.	5
	$\overline{12}$
Е.	7
	12

2. In the spring semester of her math class, Katie's test scores were 108, 81, 79, 99, 85, and 82. What was her average test score in the spring semester?

F.	534
G.	108
H.	89
J.	84
К.	80

- 3. Gregor works as a political intern and receives a monthly paycheck. He spends 20% of his paycheck on rent and deposits the remainder into a savings account. If his deposit is \$3,200, how much does he receive as his monthly pay?
 - A.\$ 4,000B.\$ 5,760
 - **C.** \$ 7,200
 - **D.** \$ 8,000
 - **E.** \$ 17,000
- 4. A size 8 dress the usually sells for \$60 is on sale for 30% off. Victoria has a store credit card that entitles her to an additional 10% odd the reduced price of any item in the store. Excluding sales tax, what is the price Victoria pays for the dress?

F.	\$ 22.20
G.	\$ 24.75
H.	\$ 34.00
J.	\$ 36.00
К.	\$ 37.80

- 5. Erin and Amy are playing poker. At a certain point in the game, Erin has 3 more chips than Amy. On the next hand, Erin wins 4 chips from Amy. Now how many more chips does Erin have than Amy?
 - A. -1 B. 1 C. 7
 - **D.** 11 **E.** 14
- 6. If y = 4, what does |1 y| = ?
 - F.
 -5

 G.
 -3

 H.
 3
 - **H.** 3 **J.** 4
 - **J.** 4 **K.** 5

Do Your Figuring Below

What is the value of $\frac{2x+4}{3x}$ when $x = \frac{1}{6}$? $4\frac{1}{3}$ А. 2 <u>26</u> B. C. 3 D. 12 E. 24

If you drive 60 miles at 90 miles an hour, how 8. many minutes will the trip take you?

F.	15
G.	30
H.	40
J.	60
K.	90

What is the product of the solutions of the expression $x^2 - 5x - 14 = 0$? 9.

A.	-14
B.	-2
C.	0
D.	5
E.	7

10. For all real value of y, 3-2(4-y) = ?

F.	-2y-9
G.	-2y+8
H.	-2y-1
J.	2y - 5
К.	2y + 11

CONTINUE TO NEXT PAGE

7.

11. How many prime numbers are between 20 and 30?

A.	1
B.	2
C.	3
D.	4
Е.	5

12. A candy jar contains 20 candies: 8 are orange, 7 are green, and 5 are red. Two candies are picked at random and eaten. If both of these are orange, what is the probability that the next candy, picked at random, is also orange?

F.	3
	$\overline{20}$
G.	1
	4
H.	3
	$\overline{10}$
J.	1
	$\overline{3}$
K.	2
	$\overline{5}$

13. In a shipment of 10,000 headlights, 5% are defective. What is the ratio of defective headlights to nondefective headlights?

A.	1
	19
B.	1
	$\overline{20}$
C.	19
	1
D.	20
	1
Е.	1
	5
	5

^{14.} Which of the following is equal to $\sqrt{20}$ $\sqrt{3}$?

F.	$2\sqrt{30}$
G.	$2\sqrt{15}$
H.	$4\sqrt{15}$
J.	$3\sqrt{10}$
K.	$20\sqrt{3}$

15. If you travel 6.2 miles in 15 minutes, what was your average speed in miles per hour?

1.55
15.5
18.6
24.8
93.0

16.

If $\frac{8}{0.25}$ is expressed as a fraction in lower terms, what number will be in the denominator?

F.	2
G.	4
H.	5
J.	8
K.	32

5

17. The choices for an ice cream sundae are as follows: chocolate or vanilla ice cream; hot fudge, strawberry, or butterscotch topping; and toasted almonds, cherry, or sprinkles as decoration. If you know that your sundae will have on ice cream, one topping, and one decoration, how many different choices for a sundae do you have?

A.	6
B.	8
C.	9
D.	12
E.	18

- 18. Yan needs \$2.37 in postage to mail a letter. If he has 60-cent, 27-cent, 23-cent, 5-cent and 1-cent stamps, as least 10 of each, what is the smallest number of stamps he can use that will get him the exact postage he needs?
 - F.
 6

 G.
 7

 H.
 8

 J.
 9

 K.
 13
- 19. A typing class in elementary school is divided into 3 groups. The Red Robins, with 6 students, has an average typing speed of 60 words per minute. The Blue Wax Bills, with 10 students, has an average typing speed of 45 words per minute, The Gold Finches, with 16 students, has an average typing speed of 30 words per minute. Which of the following is closest to the average (arithmetic mean) of the typing speeds, in words per minute, for the class?

A.	27.3
B.	32.0
C.	40.3
D.	45.0
Е.	55.7

20. In a certain election, several students collected signatures to place a candidate on the ballot. Unfortunately, 25% of the signatures were thrown out for being invalid. Then a further 20% of those remaining were thrown out. What percent of the original was left?

F.	40%
G.	45%
H.	50%
J.	55%
К.	60%

Answers: 1.D 2.H 3.A 4.K 5.C 6.H 7.C 8.H 9.A 10.J 11.B 12.J 13.A 14.G 15. D 16.F 17.E 18.H 19.C 20.K